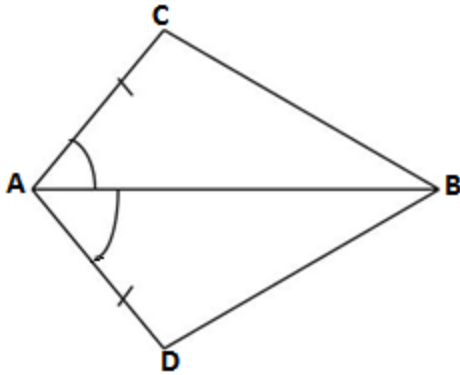


Triangles: NCERT Class 9 CBSE

Exercise 7.1

Q1. In quadrilateral ACBD, $AC = AD$, and AB bisect $\angle A$ (see the given figure). Show that $\triangle ABC \cong \triangle ABD$. What can you say about BC and BD?



Ans.

GIVEN: In quadrilateral ACBD, $AC = AD$

AB is the bisector of $\angle A$

So, $\angle BAC = \angle DAB$

TO PROVE: $\triangle ABC \cong \triangle ABD$

PROOF: In $\triangle ABC$ and $\triangle ABD$

We have

$AC = AD$ (given)

$AB = AB$ (common)

$\angle BAC = \angle DAB$ (given)

$\triangle ABC \cong \triangle ABD$ (SAS rule)

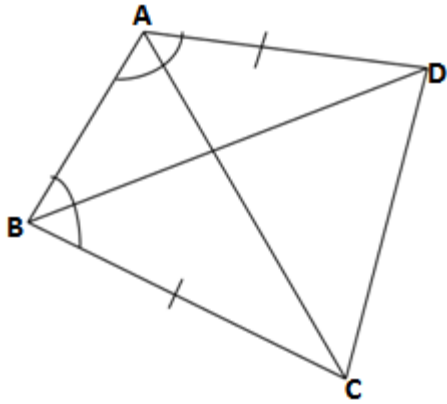
$BC = BD$ (by CPCT)

Q2. ABCD is a quadrilateral in which $AD = BC$ and $\angle DAB = \angle CBA$ (see the given figure). Prove that

(i) $\triangle ABD \cong \triangle BAC$

(ii) $BD = AC$

(iii) $\angle ABD = \angle BAC$



Ans.

(i) **GIVEN:** ABCD is a quadrilateral

$AD = BC$ and $\angle DAB = \angle CBA$

TO PROVE: $\triangle ABD \cong \triangle BAC$

PROOF: In $\triangle ABD$ and $\triangle BAC$

$AD = BC$ (given)

$AB = AB$ (common)

$\angle DAB = \angle CBA$

$\triangle ABD \cong \triangle BAC$ (SAS)

Hence proved

(ii) $BD = AC$ (By CPCT)

(iii) $\angle ABD = \angle BAC$ (By CPCT)

Q3. AD and BC are equal perpendiculars to a line segment AB (see the given figure). Show that CD bisects AB.

 $AB \perp BC$ and $AB \perp BC$

$$\therefore \angle OBC = \angle OAD = 90^\circ$$

TO PROVE: CD bisects AB i.e $AO = BO$

PROOF: In $\triangle AOD$ and $\triangle BOD$

Since BOA and COD is a line

$\angle DOA = \angle BOC$ (vertically opposite angle)

$$AD = BC \text{ (Given)}$$

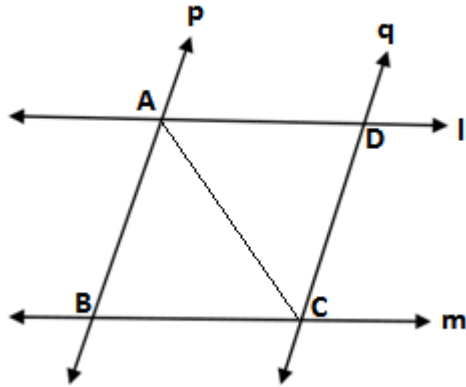
$$\angle OBC = \angle OAD = 90^\circ \text{ (given)}$$

$$\triangle BOC \cong \triangle AOD (\text{AAS})$$

$$AO = BO \text{ (By CPCT)}$$

Hence Proved

Q4. l and m are two parallel lines intersected by another pair of parallel lines p and q (see the given figure). Show that $\triangle ABC \cong CDA$.



Ans.

GIVEN: $p \parallel q$ and $l \parallel m$

TO PROVE: $\triangle ABC \cong \triangle CDA$

PROOF: In the figure

$l \parallel m$ and AC is the transversal (given)

So, $\angle DAC = \angle ACB$ (alternate angles)

$p \parallel q$ and AC is the transversal (given)

$\angle BAC = \angle ACD$ (alternate angles)

$AC = AC$ (given)

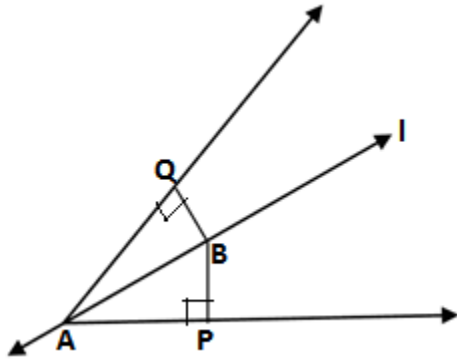
$\triangle ABC \cong \triangle CDA$ (ASA rule)

Hence proved

Q5. Line l is the bisector of an angle $\angle A$ and B is any point on l , BP and BQ are perpendiculars from B to the arms of $\angle A$ (see the given figure). Show that

(i) $\triangle APB \cong \triangle AQB$

(ii) $BP = BQ$ or B is equidistant from the arms of $\angle A$



Ans.

(i) **GIVEN:** ,BP and BQ are perpendiculars from B to the arms of $\angle A$

$$\therefore \angle AQB = \angle APB = 90^\circ$$

Line l is the bisector of an angle $\angle A$ and

$$\therefore \angle QAB = \angle PAB$$

TO PROVE: $\triangle APB \cong \triangle AQB$

PROOF: $\angle AQB = \angle APB = 90^\circ$ (given)

$AB = AB$ (common)

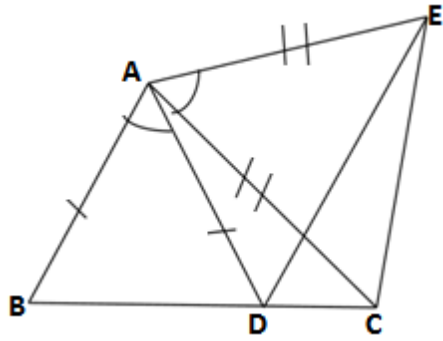
$$\angle QAB = \angle PAB \text{ (given)}$$

$\triangle APB \cong \triangle AQB$ (AAS rule)

(ii) $BP = BQ$ (by CPCT)

Hence proved

Q6. In the given figure, $AC = AE$, $AB = AD$ and $\angle BAD = \angle EAC$. Show that $BC = DE$.



Ans.

GIVEN: $AC = AE$

$AB = AD$

$\angle BAD = \angle EAC$

TO PROVE: $BC = DE$

PROOF: We have to prove $BC = DE$, which are sides of the triangle $\triangle ABC$ and $\triangle ADE$

In triangles $\triangle ABC$ and $\triangle ADE$

$AB = AD$ (given)

$AC = AE$ (given)

$\angle BAD = \angle EAC$ (given)

Adding both sides $\angle DAC$

$\angle BAD + \angle DAC = \angle EAC + \angle DAC$

$\angle BAC = \angle DAE$ (proved)

$\triangle ABC \cong \triangle ADE$ (SAS rule)

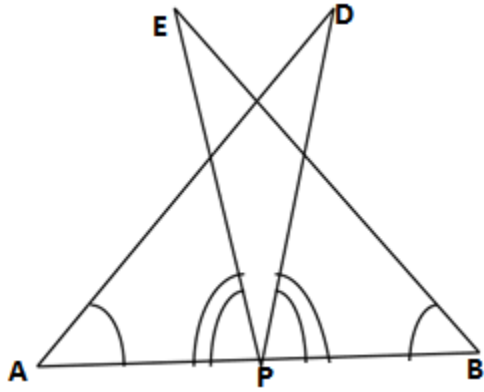
$BC = DE$ (by CPCT)

Hence proved

Q7. AB is a line segment and p is its midpoint. D and E are points on the same sides of AB such that $\angle BAD = \angle ABE$ and $\angle EPA = \angle DPB$ (see the given figure). Show that

(i) $\triangle DAP \cong \triangle EBP$

(ii) $AD = BE$



Ans.(i)

GIVEN: $\angle DAP = \angle EBP$

$\angle EPA = \angle DPB$

P is the mid point of AB

$\therefore AP = BP$

TO PROVE:

(i) $\triangle DAP \cong \triangle EBP$

(ii) $AD = BE$

PROOF: In $\triangle DAP$ and $\triangle EBP$

$\angle BAD = \angle ABE$ (given)

$\angle EPA = \angle DPB$ (given)

Adding $\angle EPD$ both sides

$\angle EPA + \angle EPD = \angle DPB + \angle EPD$

$\angle APD = \angle EPB$

$AP = BP$ (given)

$\triangle DAP \cong \triangle EBP$ (ASA rule)

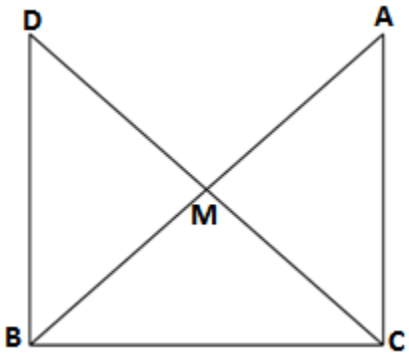
Q8. In right triangle ABC, right angled at C, M is the mid point of hypotenuse AB, C is joined to M and produced to a point D such that $DM = CM$. Point D is joined to point B (see the given figure). Show that

(i) $\triangle AMC \cong \triangle BMD$

(ii) $\angle DBC$ is a right angle

(iii) $\triangle DBC \cong \triangle ACB$

(iv) $CM = \frac{1}{2}AB$



Ans.

(i) **GIVEN:** $\triangle ABC$ is a right triangle, $\angle C = 90^\circ$

M is the midpoint of AB

$\therefore BM = AM$

$AM = AB/2$

$DM = CM$

TO PROVE: $\triangle AMC \cong \triangle BMD$

PROOF: $DM = CM$ (given)

$BM = AM$ (given)

$\angle BMD = \angle AMC$ (Vertically opposite angle)

$\triangle AMC \cong \triangle BMD$ (SAS rule)

Hence proved

(ii) Since $\triangle AMC \cong \triangle BMD$ (proved)

$\angle DBM = \angle CAM$ (By CPCT)

$\angle DBM$ and $\angle CAM$ are alternate angles

$\therefore DB \parallel AC$

$\angle DBC + \angle ACB = 180^\circ$ (co-interior angles)

$\angle ACB = 90^\circ$

$\angle DBC + 90^\circ = 180^\circ$

$\angle DBC = 90^\circ$

Hence proved

(iii) Since $\triangle AMC \cong \triangle BMD$ (proved)

$BD = AC$ (By CPCT)

$BC = BC$ (common)

$\angle DBC = \angle ACB = 90^\circ$ (Proved above)

$\triangle DBC \cong \triangle ACB$ (SAS rule)

proved above

(iv) $CM = DM$ (given)

$CM + DM = DC$

$CM + CM = DC$

$2CM = DC$

$CM = \frac{1}{2} DC$

Since we have proved

$$\triangle DBC \cong \triangle ACB$$

So, $DC = AB$ (by CPCT)

Therefore

$$CM = \frac{1}{2} AB$$

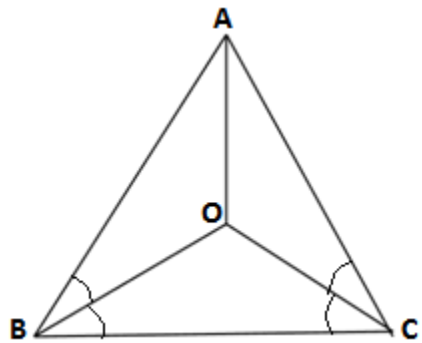
Hence proved

Exercise 7.2

Q1. In an isosceles triangle ABC , with $AB = AC$, the bisector of angle $\angle B$ and $\angle C$, intersect each other at O . Join A to O . Show that:

(i) $OB = OC$ (ii) AO bisects $\angle A$

Ans.



GIVEN: In $\triangle ABC$

$$AB = AC$$

BO is bisector of $\angle B$ and CO is bisector of $\angle C$

TO PROVE: (i) $OB = OC$ (ii) AO bisects $\angle A$

PROOF: In $\triangle ABC$

$$AB = AC \text{ (given)}$$

$\angle ABC = \angle ACB$ (angles opposite to equal sides)

It is given to us that BO is bisector of $\angle B$ and CO is bisector of $\angle C$

$$\frac{1}{2}(\angle ABC) = \frac{1}{2}(\angle ACB)$$

$$\angle OBC = \angle OCB$$

OB = OC (sides opposite to equal angles)

Hence proved

(ii) OB = OC (proved above)

AO = AO (common)

AB = AC (given)

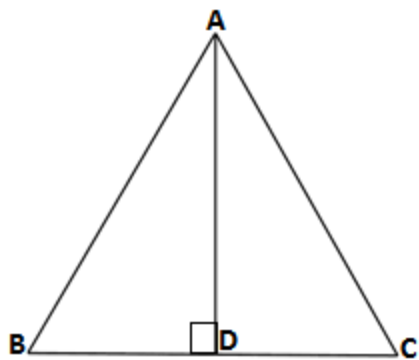
$\triangle ABO \cong \triangle ACO$ (SSS rule)

$\angle OAB = \angle OCA$ (by CPCT)

Therefore AO is the bisector of $\angle A$.

Hence proved

Q2. In $\triangle ABC$, AD is perpendicular bisector of BC (see the given figure). Show that $\triangle ABC$ is an isoscles triangle in which $AB = AC$.



Ans.

GIVEN: In $\triangle ABC$, AD is perpendicular bisector of BC

$$\therefore BD = DC$$

$$\angle ADB = \angle ADC = 90^\circ$$

TO PROVE: $AB = AC$

PROOF: In $\triangle ABD$ and $\triangle ACD$

$$\angle ADB = \angle ADC = 90^\circ \text{ (given)}$$

$$AD = AD \text{ (common)}$$

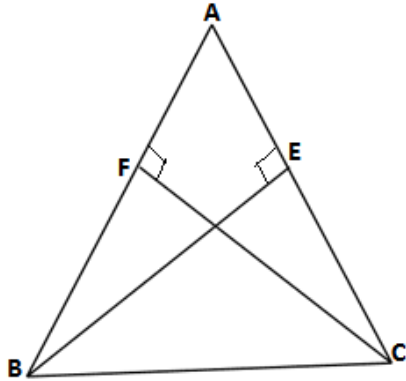
$$BD = DC \text{ (given)}$$

$$\triangle ABD \cong \triangle ACD \text{ (SAS rule)}$$

$$AB = AC \text{ (by CPCT)}$$

Hence $\triangle ABC$ is an isosceles triangle in which $AB = AC$

Q3. ABC is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see the given figure). Show that these altitudes are equal.



Ans.

GIVEN: $\triangle ABC$ in which $AC = AB$

$$CF \perp AB \text{ and } BE \perp AC$$

$$\therefore \angle AFC = \angle AEB = 90^\circ$$

TO PROVE: $CF = BE$

PROOF: $AC = AB$ (given)

$\angle AFC = \angle AEB = 90^\circ$ (given)

$\angle A = \angle A$ (common)

$\triangle AEB \cong \triangle AFC$ (AAS rule)

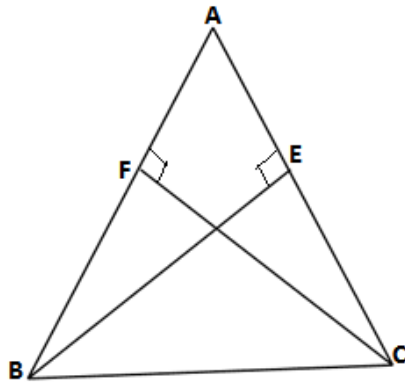
$BE = CF$ (by CPCT)

Hence proved

Q4. $\triangle ABC$ is a triangle in which altitudes BE and CF to sides AC and AB are equal (see the given figure). Show that.

(i) $\triangle ABE \cong \triangle ACF$

(ii) $AB = AC$ i.e. $\triangle ABC$ is an isosceles triangle



Ans.

GIVEN: $\triangle ABC$ in which $BE = CF$

$CF \perp AB$ and $BE \perp AC$

$\therefore \angle AFC = \angle AEB = 90^\circ$

TO PROVE: $AC = AB$

(i) **PROOF:** $BE = CF$ (given)

$\angle AFC = \angle AEB = 90^\circ$ (given)

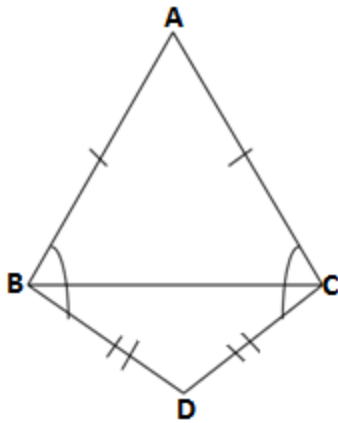
$$\angle A = \angle A \text{ (common)}$$

$$\triangle AEB \cong \triangle AFC \text{ (AAS rule)}$$

$$(ii) AC = AB \text{ (by CPCT)}$$

Hence proved

Q5. ABC and DBC are two isosceles triangles on the same base BC (see the given figure). Show that $\angle ABD = \angle ACD$.



Ans.

GIVEN: $\triangle ABC$ in which $AB = AC$

$\triangle DBC$ in which $BD = DC$

TO PROVE: $\angle ABD = \angle ACD$

PROOF: In $\triangle ABC$

$$AB = AC \text{ (given)}$$

$$\angle ABC = \angle ACB \dots(i) \text{ (angles opposite to equal sides)}$$

$$BD = DC$$

$$\angle DBC = \angle DCB \dots(ii) \text{ (angles opposite to equal sides)}$$

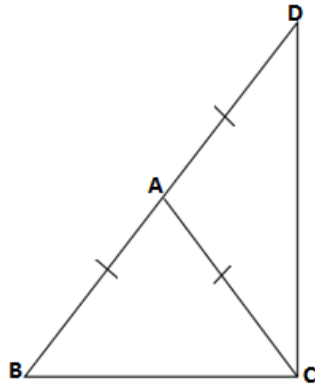
Adding equation (i) and (ii)

$$\angle ABC + \angle DBC = \angle ACB + \angle DCB$$

$$\angle ABD = \angle ACD$$

Hence proved

Q6. $\triangle ABC$ is an isosceles triangle in which $AB = AC$, side BA is produced to D such that $AD = AB$ (see the given figure). Show that $\angle BCD$ is a right angle.



Ans.

GIVEN: $AB = AC$

$AD = AB$

TO PROVE: $\angle BCD = 90^\circ$

PROOF : $AB = AC$ (given)

$\angle ABC = \angle ACB$ (angles opposite to equal sides)

Applying the angle sum property in $\triangle ABC$

$$\angle ABC + \angle BAC + \angle ACB = 180^\circ$$

$$\angle BAC = 180^\circ - (\angle ABC + \angle ACB)$$

$\angle BAC$ and $\angle DAC$ are linear pair

$$\text{So, } \angle BAC + \angle DAC = 180^\circ$$

$$180^\circ - (\angle ABC + \angle ACB) + \angle DAC = 180^\circ$$

$$\angle DAC = \angle ABC + \angle ACB = \angle ACB + \angle ACB = 2\angle ACB$$

$$\angle ACB = \frac{1}{2} \angle DAC \dots (i)$$

$AD = AC$ (given)

$\angle ADC = \angle ACD$ (angles opposite to equal sides)

Applying the angle sum property in $\triangle ABC$

$$\angle ADC + \angle ACD + \angle DAC = 180^\circ$$

$$\angle ACD + \angle ACD + \angle DAC = 180^\circ$$

$$2\angle ACD + \angle DAC = 180^\circ$$

$$\angle DAC = 180^\circ - 2\angle ACD$$

$$\angle ACD = 90^\circ - \frac{1}{2} \angle DAC \dots\dots(ii)$$

Adding equation (i) and (ii)

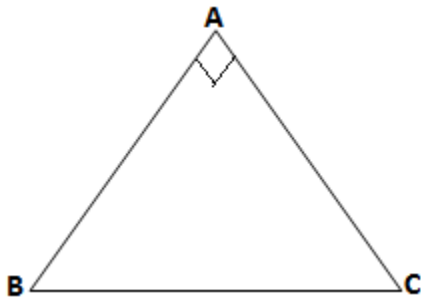
$$\angle ACB + \angle ACD = \frac{1}{2} \angle DAC + 90^\circ - \frac{1}{2} \angle DAC$$

$$\angle BCD = 90^\circ$$

Hence $\triangle BCD$ is right triangle

Q7. ABC is a right triangle in which $\angle A = 90^\circ$ and $AB = AC$. Find $\angle B$ and $\angle C$.

Ans.



We are given triangle ABC in which

$$\angle A = 90^\circ$$

$$AB = AC$$

$\angle B = \angle C$ (angles opposite to equal sides)

$$\angle B + \angle C + \angle A = 180^\circ$$

$$\angle B + \angle B + 90^\circ = 180^\circ$$

$$2\angle B + 90^\circ = 180^\circ$$

$$2\angle B = 90^\circ$$

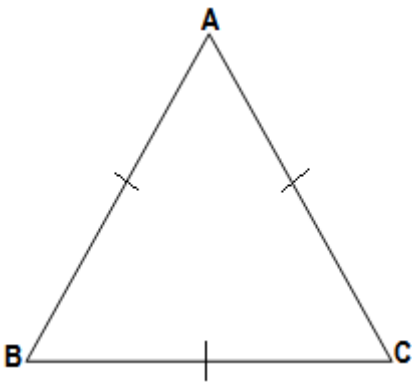
$$\angle B = 45^\circ$$

$$\angle C = 45^\circ$$

Hence both of the angles $\angle B$ and $\angle C$ are of 45°

Q8. Show that the angles of an equilateral triangle are 60° each.

Ans.



We are given that $\triangle ABC$ is an equilateral triangle

$AB = AC$ (sides of equilateral triangle)

$\angle C = \angle B$ (i)(angles opposite to equal sides)

$BC = AC$ (sides of equilateral triangle)

$\angle B = \angle A$ (ii)(angles opposite to equal sides)

From equation (i) and (ii)

$$\angle A = \angle B = \angle C$$

Applying angle sum property of the triangle in $\triangle ABC$

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle A + \angle A = 180^\circ$$

$$3\angle A = 180^\circ$$

$$\angle A = 180^\circ / 3$$

$$\angle A = 60^\circ$$

$$\therefore \angle A = \angle B = \angle C = 60^\circ$$

Therefore angles of an equilateral triangle are 60° each.

Exercise 7.3

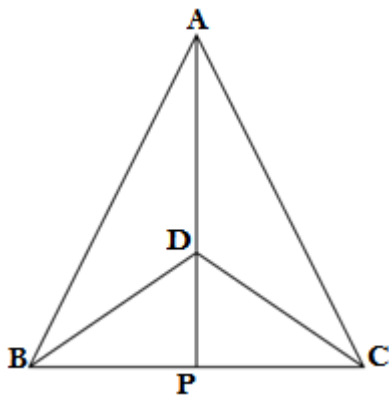
Q1. $\triangle ABC$ and $\triangle DBC$ are two isosceles on the same base BC and vertices A and D are on the same side of BC (see the given figure). If AD is extended to intersect BC at P , show that

(i) $\triangle ABD \cong \triangle ACD$

(ii) $\triangle ABP \cong \triangle ACP$

(iii) AP bisects $\angle A$ and as well as $\angle D$

(iv) AP is the perpendicular bisector of BC



Ans.

GIVEN: $\triangle ABC$ and $\triangle DBC$ are two isosceles with a common base BC

In which $AB = AC$ and $AD = DC$

(i) TO PROVE: $\triangle ABD \cong \triangle ACD$

PROOF: $AB = AC$ (given)

$BD = CD$ (given)

$AD = AD$ (common)

$\triangle ABD \cong \triangle ACD$ (SSS rule)

Hence proved

(ii) TO PROVE: $\triangle ABP \cong \triangle ACP$

PROOF: $AB = AC$ (given)

$AP = AP$ (common)

Since we have already proved $\triangle ABD \cong \triangle ACD$

$\therefore \angle BAP = \angle CAP$ (By CPCT)

$\triangle ABP \cong \triangle ACP$ (SAS rule)

Hence proved

(iii) TO PROVE: AP bisects $\angle A$ and as well as $\angle D$

PROOF: In $\triangle DPB$ and $\triangle DPC$

Since we have proved $\triangle ABD \cong \triangle ACD$ and $\triangle ABP \cong \triangle ACP$

$\therefore BD = DC$ (By CPCT) and $BP = PC$ (CPCT)

$DP = DP$ (common)

$\triangle DPB \cong \triangle DPC$

$\angle DPB = \angle DPC$ (By CPCT)...(i)

And it is already proved $\triangle ABD \cong \triangle ACD$

$\angle BAD = \angle DAC$ (By CPCT)....(*ii)

From (i) and (ii) it is clear that AP bisects $\angle A$ and as well as $\angle D$

Hence proved

(iv) TO PROVE: AP is the perpendicular bisector of BC

PROOF: Since we have proved $\triangle ABP \cong \triangle ACP$

Therefore $\angle APB = \angle APC$ (By CPCT)

$BP = PC$ (By CPCT).....(i)

$\angle APB + \angle APC = 180^\circ$

$\angle APB + \angle APB = 180^\circ$

$2 \angle APB = 180^\circ$

$\angle APB = 90^\circ$

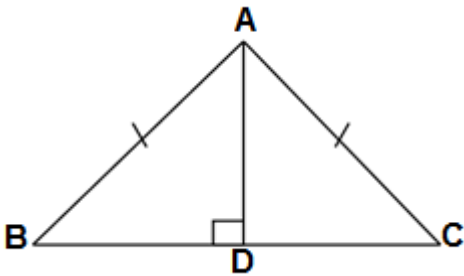
$\therefore AP \perp BC$(ii)

From (i) and (ii), it is cleared that AP is a perpendicular bisector of BC

Hence proved

Q2. AD is an altitude of an isosceles triangle ABC in which $AB = AC$. Show that (i) AD bisects BC (ii) AD bisects $\angle A$.

Ans.



GIVEN: An isosceles triangle $\triangle ABC$ in which $AB = AC$

AD is the altitude of the isosceles triangle

$$\therefore \angle ADC = \angle ADB = 90^\circ$$

TO PROVE: (i) AD bisects BC

In $\triangle ABD$ and $\triangle ACD$

$$AD = AD \text{ (common)}$$

$$AB = AC \text{ (given)}$$

$$\angle ADC = \angle ADB = 90^\circ (AD \perp BC)$$

$$\triangle ABD \cong \triangle ACD \text{ (RHS rule)}$$

$$BD = DC \text{ (By CPCT)}$$

Hence AD bisects BC

(ii) TO PROVE: AD bisects $\angle A$.

Since we have proved $\triangle ABD \cong \triangle ACD$

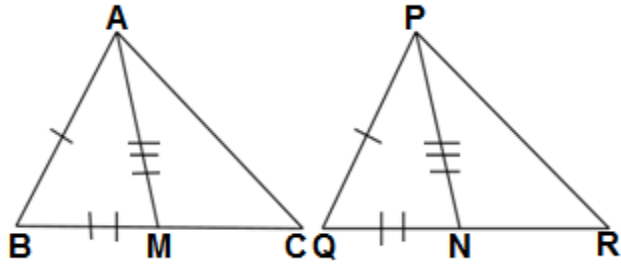
$$\therefore \angle BAD = \angle DAC \text{ (By CPCT)}$$

Therefore AD bisects $\angle A$

Q3. Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$ see the given figure. Show that.

$$(i) \triangle ABM \cong \triangle PQN$$

$$(ii) \triangle ABC \cong \triangle PQR$$



Ans.

GIVEN: In $\triangle ABC$ and $\triangle PQR$

$$AB = PQ$$

$$BC = QR$$

$$AM = PN$$

TO PROVE: (i) $\triangle ABM \cong \triangle PQN$

PROOF: $AB = PQ$ (given)

$$AM = PN \text{ (given)}$$

$$BC = QR \text{ (given)}$$

Since AM is the median of the triangle $\triangle ABC$ and PN is the median of the triangle $\triangle PQR$

$$\therefore BC/2 = QR/2$$

$$BM = QN$$

$$\triangle ABM \cong \triangle PQN \text{ (SSS rule)}$$

Hence proved

TO PROVE (ii) $\triangle ABC \cong \triangle PQR$

PROOF: Since we have already proved $\triangle ABM \cong \triangle PQN$

$\therefore \angle ABM = \angle PQN$ (by CPCT)

$AB = PQ$ (given)

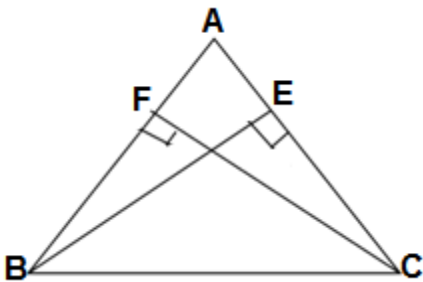
$BC = QR$ (given)

$\triangle ABM \cong \triangle PQN$ (SAS rule)

Hence proved

Q4. BE and CF are two equal altitudes of a triangle ABC. Using the RHS congruence rule, prove that the triangle ABC is isosceles.

Ans.



GIVEN: In $\triangle ABC$, in which two altitudes BE and CF are equal

$BE = CF$

$\angle CFB = \angle CEB = 90^\circ$

TO PROVE: triangle ABC is isosceles

In $\triangle CFB$ and $\triangle BEC$

The hypotenuse of both right triangles is common

$BC = BC$ (common)

$\angle CFB = \angle CEB = 90^\circ$ (BE and CF are altitudes of both triangles)

$BE = CF$ (equal)

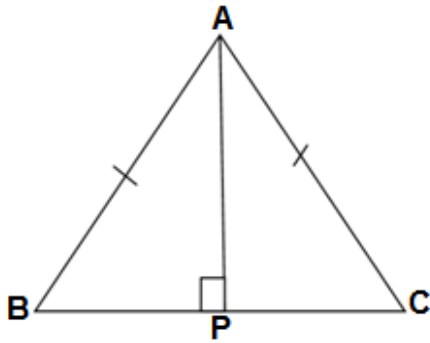
$\triangle CFB \cong \triangle BEC$ (RHS rule)

$$\angle B = \angle C \text{ (by CPCT)}$$

$$AB = AC \text{ (opposite sides of equal triangles)}$$

Q5. ABC is an isoscles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.

Ans.



GIVEN: In triangle ABP and triangle ACP

$$AB = AC$$

$$\angle APB = \angle APC = 90^\circ \text{ (AP } \perp \text{ BC)}$$

TO PROVE: $\angle B = \angle C$

PROOF: In $\triangle ABP$ and $\triangle ACP$

$$AB = AC \text{ (given)}$$

$$AP = AP \text{ (common)}$$

$$\angle APB = \angle APC = 90^\circ \text{ (given)}$$

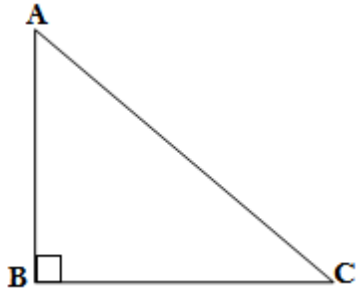
$$\triangle ABP \cong \triangle ACP \text{ (RHS rule)}$$

$$\angle B = \angle C \text{ (by CPCT)}$$

Hence proved

Q1. Show that in a right-angled triangle, the hypotenuse is the longest side.

Ans.



GIVEN: $\triangle ABC$ is a right triangle, let $\angle B = 90^\circ$

TO PROVE: Hypotenuse is the largest side in a right triangle

PROOF: $\angle B = 90^\circ$ (given)

$$\angle A + \angle B + \angle C = 180^\circ \text{ (angle sum property of the triangle)}$$

$$\angle A + 90^\circ + \angle C = 180^\circ$$

$$\angle A + \angle C = 180^\circ - 90^\circ = 90^\circ$$

$\angle A$ and $\angle C$ must be acute angle

$$\therefore \angle A < 90^\circ \text{ and } \angle C < 90^\circ$$

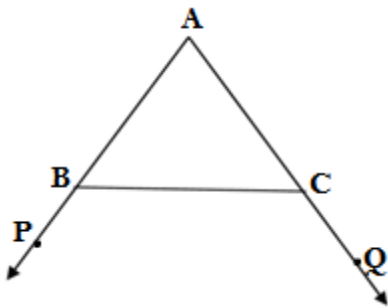
Therefore $\angle B$ is the largest angle

So, $\angle B > \angle A$ and $\angle B > \angle C$

$AC > BC$ and $AC > AB$ (in a triangle side opposite to larger angle is longer)

Hence AC(hypotenuse) is the largest side in a right triangle

Q2. In the given figure sides AB and AC of $\triangle ABC$ are extended to points P and Q respectively. Also $\angle PBC < \angle QCB$. Show that $AC > AB$.



Ans.

GIVEN: In the fig. $\angle PBC < \angle QCB$

TO PROVE: $AC > AB$

PROOF: $\angle PBC < \angle QCB$ (given)

$$\angle ABC + \angle PBC = 180^\circ \text{ (linear pair)}$$

$$\angle PBC = 180^\circ - \angle ABC \text{(i)}$$

$$\angle ACB + \angle QCB = 180^\circ \text{ (linear pair)}$$

$$\angle QCB = 180^\circ - \angle ACB \text{(ii)}$$

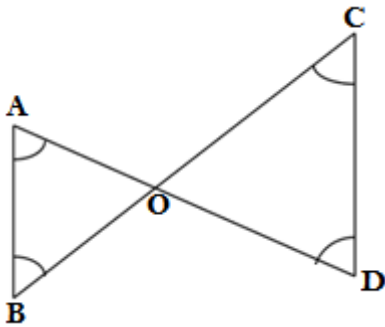
From equation (i) and equation (ii)

$$180^\circ - \angle ABC < 180^\circ - \angle ACB$$

$$\angle ABC > \angle ACB$$

$AC > AB$ (side opposite to larger angle is greater)

Q3.In the given figure , $\angle B < \angle A$, and $\angle C < \angle D$. Show that $AD < BC$.



Ans.

GIVEN: $\angle B < \angle A$, and $\angle C < \angle D$

TO PROVE: $AD < BC$

PROOF: $\angle B < \angle A$ (given)

$OA < OB$(i) (side opposite to larger angle is greater)

$\angle C < \angle D$

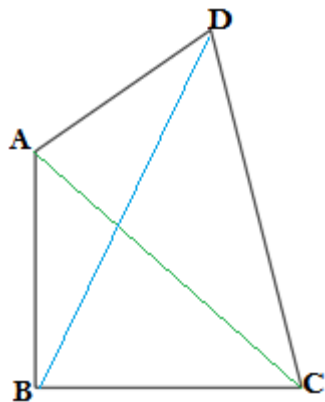
$OD < OC$...(ii) (side opposite to larger angle is greater)

From equation (i) and equation (ii)

$OA + OD < OB + OC$

$AD < BC$ (from figure), Hence proved

Q4. AB and CD are respectively smallest and the longest side of quadrilateral $ABCD$ (see the given figure). Show that $\angle A > \angle C$ and $\angle B > \angle D$.



Ans.

GIVEN: AB and CD are respectively smallest and the longest side of quadrilateral ABCD

COSTRUCTION: Joining A to C and B to D

TO PROVE: (i) $\angle A > \angle C$ (ii) $\angle B > \angle D$.

(i) PROOF: In $\triangle ABC$

$BC > AB$ (AB is the smallest side in ABCD)

$\angle BAC > \angle ACB$ (i) (side opposite to larger angle is grater)

In $\triangle ADC$

$CD > AD$ (CD is the largest side in ABCD)

$\angle DAC > \angle ACD$(ii)

Adding equation (i) and (ii)

$\angle BAC + \angle DAC > \angle ACB + \angle ACD$

$\angle A > \angle C$, Hence proved

PROOF: (ii) $\angle B > \angle D$

In $\triangle ABD$

$AD > AB$ (AB is the smallest side in ABCD)

$\angle ABD > \angle ADB$ (i) (side opposite to larger angle is grater)

In $\triangle ADC$

$CD > BC$ (CD is the largest side in $ABCD$)

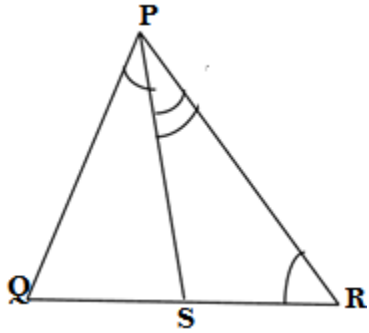
$\angle DBC > \angle BDC$(ii)

Adding equation (i) and (ii)

$\angle ABD + \angle DBC > \angle ADB + \angle BDC$

$\angle B > \angle D$, Hence proved

Q5. In the given figure , $PR > PQ$ and PS bisects $\angle QPR$, prove that $\angle PSR > \angle PSQ$.



Ans.

GIVEN: $PR > PQ$

PS bisects $\angle QPR$

$\angle QPS = \angle SPR$

TO PROVE: $\angle PSR > \angle PSQ$

PROOF: $PR > PQ$ (given)

$\angle Q > \angle R$ (side opposite to larger angle is greater)

In $\triangle PQS$

$\angle Q + \angle QPS + \angle PSQ = 180^\circ$ (angle sum property of the triangle)

$$\angle Q = 180^\circ - (\angle QPS + \angle PSQ) \dots (i)$$

In $\triangle PSR$

$\angle R + \angle SPR + \angle PSR = 180^\circ$ (angle sum property of the triangle)

$$\angle R = 180^\circ - (\angle SPR + \angle PSR) \dots (ii)$$

From (i) and (ii)

$$180^\circ - (\angle QPS + \angle PSQ) > 180^\circ - (\angle SPR + \angle PSR)$$

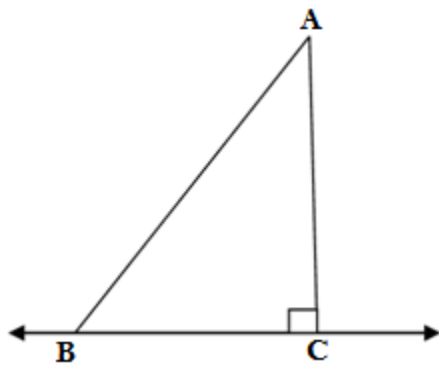
$$\angle SPR + \angle PSR > \angle QPS + \angle PSQ$$

Since PS bisects $\angle P$, $\angle QPS = \angle SPR$

$$\angle SPR + \angle PSR > \angle SPR + \angle PSQ$$

$\angle PSR > \angle PSQ$, Hence proved

Q6. Show that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.



Ans. Let A is an external point out of the line and $AC \perp BC$

Let BC is a line and AB is a line segment drawn from the point A on the line BC

In triangle $\triangle ABC$

$\angle B < \angle C$ (since $\angle B$ is acute angle and $\angle C = 90^\circ$)

$AC < AB$ (side opposite to larger angle is greater)

Similarly all line segments drawn from A on the line BC are larger than AC

Therefore AC is the shortest side drawn from A on BC, Hence proved

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